

Name: _____

Student #: _____

Date: _____

T.A. #: _____

Mathematics 12 Pre-Calculus
LEARNING GUIDE 5 TEST – POLYNOMIAL FUNCTIONS

***NO GRAPHING CALCULATORS PERMITTED ON THIS TEST**

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***Full marks will NOT be given for the final answer only.**

When using a calculator, you should provide a decimal answer that is correct **to at least two decimal places** (unless otherwise indicated). Such rounding should occur **only** in the final step of the solution.

1. Write an example of a polynomial function. Explain why it is a polynomial function. (2 marks)

EXAMPLE: $f(x) = 3x^2 - 2x + 1$

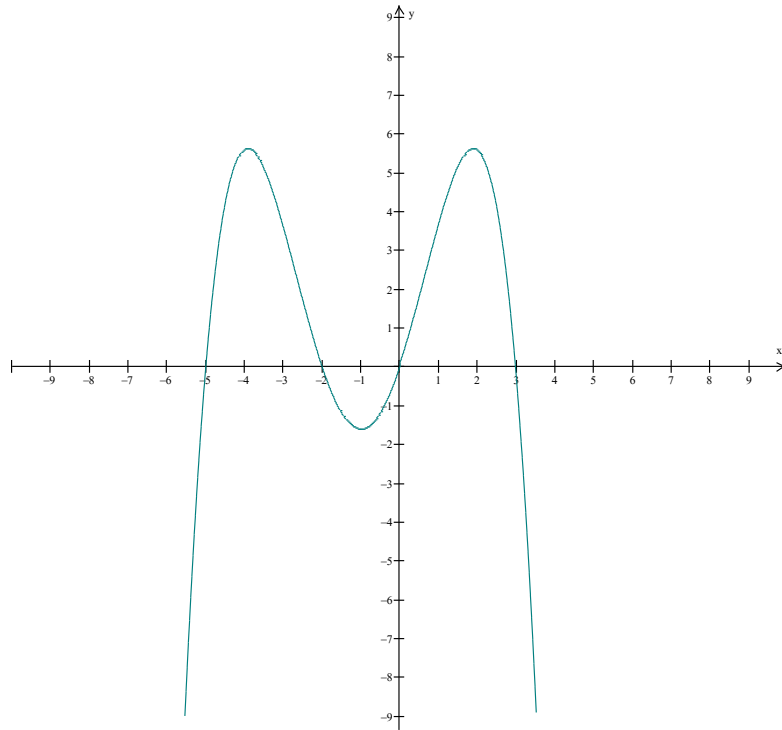
EXPONENTS ON X ARE WHOLE #'S.

2. For the polynomial function $f(x) = 7x - 3 - 8x^3$ state: (2 marks)

- a) The degree: **3**
- b) Name of the polynomial function: **CUBIC**
- c) Leading coefficient: **-8**
- d) Constant term: **-3**

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3. Given the graph below:



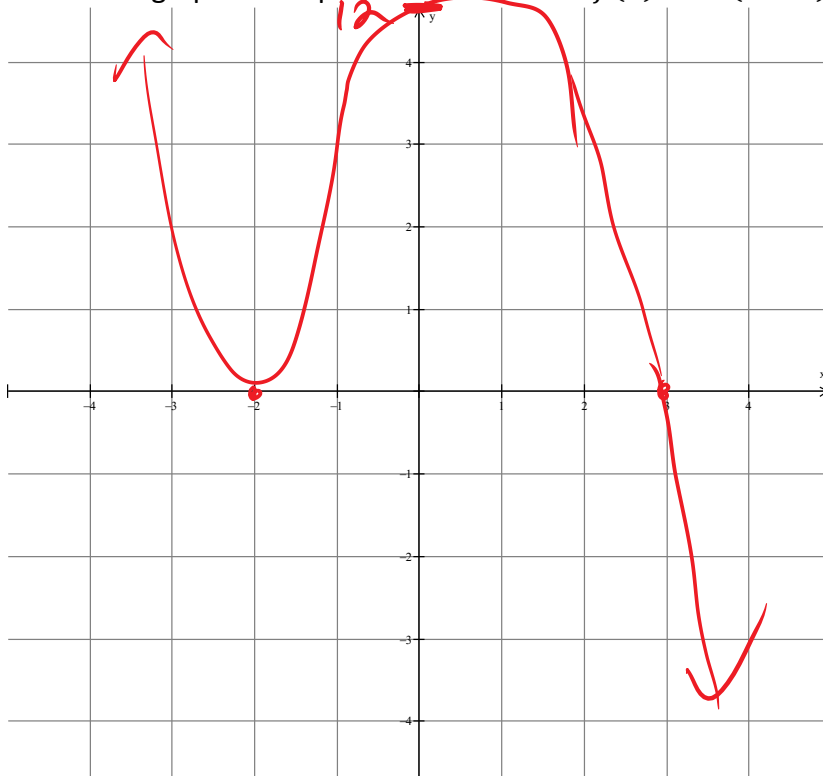
- a) What degree is this function? **4** (1 mark each)
- b) Is the leading coefficient positive or negative? **NEGATIVE**
- c) How many roots does this function have? **4**
4. Given the function $y = ax^n + 2x + b$, what are the conditions on a , n , and b for this function to have a minimum value with a negative y intercept? (3 marks)

$$a > 0$$

n IS EVEN NATURAL NUMBER (ie 2, 4, 6, ...)

$$b < 0$$

5. Sketch the graph of the polynomial function $f(x) = -(x + 2)^2(x - 3)$. (3 marks)



6. Given the function $f(x) = x^4 - 16x^2$ $f(x) = x^2(x^2 - 16)$ (4 marks)

- a) Degree and end- behavior: 4, LEFT: UP QUAD 2 RIGHT: UP QUAD 1
- b) The zeros and their multiplicity: 0 (MULT OF 2), 4, -4 (EACH MULT OF 1)
- c) The y-intercept: 0

7. Determine the quotient:

(3 marks)

$$(2x^3 + 3x^2 - 9x - 10) \div (x - 2)$$

$$\begin{array}{r|rrrr} -2 & 2 & 3 & -9 & -10 \\ & \downarrow & -4 & -14 & -10 \\ \hline x & 2 & 7 & 5 & 0 \end{array}$$

$$2x^2 + 7x + 5$$

8. Use the remainder theorem to determine the remainder when $2x^2 - 7x + 4$ is divided by $x + 2$. (1 mark)

$$2(-2)^2 - 7(-2) + 4$$

$$8 + 14 + 4 = 26$$

9. When $x^3 - kx^2 + 6$ is divided by $x - 3$, the remainder is 4. Determine k . (2 marks)

$$3^3 - k(3)^2 + 6 = 4$$

$$27 - 9k + 6 = 4$$

$$-9k = -29$$

$$k = \frac{29}{9}$$

10. For the function $f(x) = x^3 - 2x^2 - 9x + 18$

a) List the possible integral factors. (1 mark)

$$\pm 1, \pm 2, \pm 3, \pm 6, \pm 9, \pm 18$$

b) Factor fully. (2 marks)

$x + 2$ is a factor

$$\begin{array}{r|rrrr} -2 & 1 & -2 & -9 & 18 \\ & & \downarrow & -2 & \textcircled{0} & 18 \\ \hline x & 1 & \textcircled{0} & -9 & 0 \end{array}$$

$$(x-2)(x^2-9) = (x-2)(x-3)(x+3)$$

11. Show that $x + a$ is a factor of the polynomial:

$$P(x) = (x + a)^2 + (x + c)^2 - (a - c)^2$$

(3 marks)

If $x + a$ is a factor, then $-a$ is a root.

$$\begin{aligned} P(-a) &= (-a+a)^2 + (-a+c)^2 - (a-c)^2 \\ &= 0 + (a^2 - 2ac + c^2) - (a^2 - 2ac + c^2) \\ &= 0. \end{aligned}$$

Since $P(-a) = 0$, $x + a$ is a factor