

Name: _____

Student #: _____

Date: _____

T.A. #: _____

Mathematics 12 Pre-Calculus
LEARNING GUIDE 4 TEST – RADICAL FUNCTIONS

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***Full marks will NOT be given for the final answer only.**

When using a calculator, you should provide a decimal answer that is correct **to at least two decimal places** (unless otherwise indicated). Such rounding should occur **only** in the final step of the solution.

1. What transformations need to be made to the function $y = \sqrt{x}$ to obtain the graph of the function $y = -3\sqrt{2(x-1)}$? (2 marks)

REFLECT IN X

VE BAFO 3

HC BAFO $\frac{1}{2}$

RIGHT 1

2. Determine the equation of each radical function, which has been transformed from $f(x) = \sqrt{x}$ by a reflection in the x axis, a vertical compression by a factor of $\frac{1}{3}$, moved left 1 and down 2. (2 marks)

$$y = -\frac{1}{3}\sqrt{x+1} - 2$$

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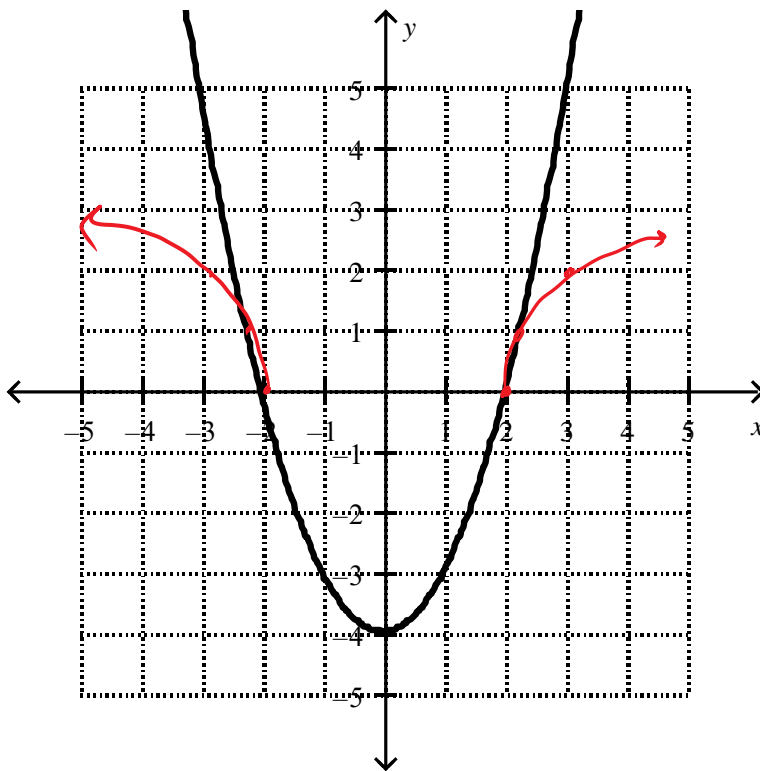
3. Determine the domain and range of the following function:

$$f(x) = -\frac{1}{5}\sqrt{3(x+1)}$$

$$D: x \geq -1$$

$$R: y \leq 0$$

4. Using each graph of $y = f(x)$, sketch the graph of $y = \sqrt{f(x)}$. (2 marks)



5. Given the function $f(x) = 8 - x^2$, identify the differences in the domains and ranges of $y = f(x)$ and $y = \sqrt{f(x)}$. (2 marks)

$$y = f(x)$$

$$D: x \in \mathbb{R}$$

$$R: y \leq 8$$

$$y = \sqrt{f(x)}$$

$$D: -2\sqrt{2} \leq x \leq 2\sqrt{2}$$

$$R: 0 \leq y \leq 2\sqrt{2}$$

6. Solve the equation $-2\sqrt{8-x} = 4$ algebraically. (2 marks)

$$\sqrt{8-x} = -2$$

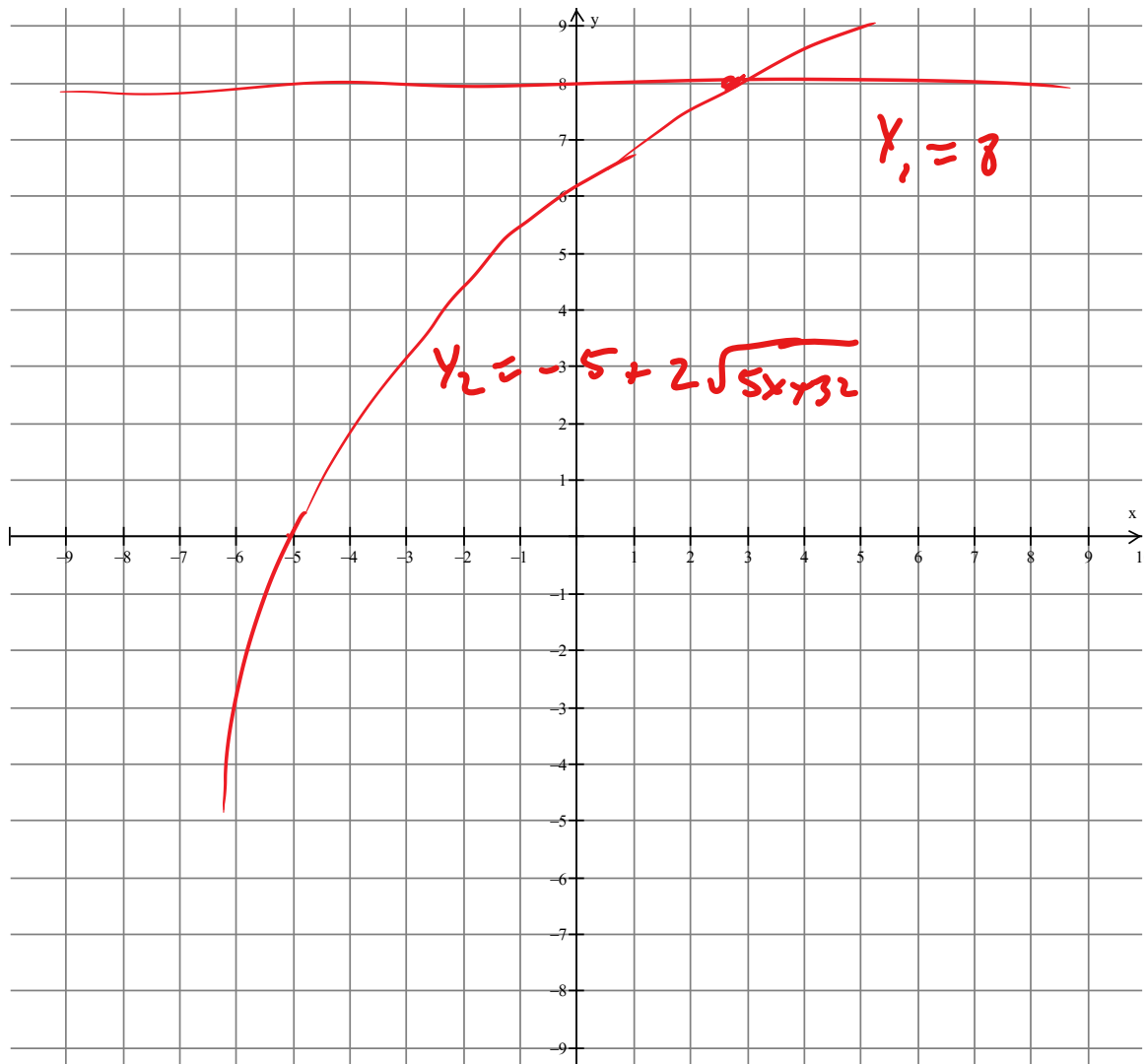
$$8-x = 4$$

$$-x = -4$$

~~$$x = 4$$~~

NO SOLUTION

7. Solve the equation $-5 + 2\sqrt{5x + 32} = 8$ graphically.



THE SOLUTION WILL BE THE X COORDINATE OF THE INTERSECTION POINT.

$$X = 2.05$$

8. The manufacturer of a new Global Positioning Satellite (GPS) system wants to predict the consumer interest in its new device. The company uses the function $I(w) = -3\sqrt{w-1} + 15$ to model the number, I , in thousands, of pre-orders for the GPS as a function of the number, w , of weeks before the GPS release date.

- a) Determine the number of pre-orders the manufacturer can expect to have 10 weeks before the release date. (1 mark)

$$\begin{aligned}
 I &= -3\sqrt{10-1} + 15 \\
 &= -3\sqrt{9} + 15 \\
 &= -9 + 15 \\
 &= 6 \quad \text{SO 6000 ORDERS}
 \end{aligned}$$

- b) Graph the function and determine the x-intercept using the graph. (1 mark)



- c) What is the meaning of the x-intercept in this context? (1 mark)

26 WEEKS PRIOR TO RELEASE, THERE WAS NO INTEREST.