

Name: _____

Student #: _____

Date: _____

T.A. #: _____

Mathematics 12 Pre-Calculus
LEARNING GUIDE 5 TEST – POLYNOMIAL FUNCTIONS

***NO GRAPHING CALCULATORS PERMITTED ON THIS TEST**

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***Full marks will NOT be given for the final answer only.**

When using a calculator, you should provide a decimal answer that is correct **to at least two decimal places** (unless otherwise indicated). Such rounding should occur **only** in the final step of the solution.

1. Write an example of a polynomial function. Explain why it is a polynomial function. (2 marks)

$$y = 5x^3 - 2x + 3 \quad \text{IS AN EXAMPLE}$$

THE EXPONENTS ARE WHOLE NUMBERS

2. For the polynomial function $f(x) = 7x^2 + 11 - 8x$ state: (2 marks)

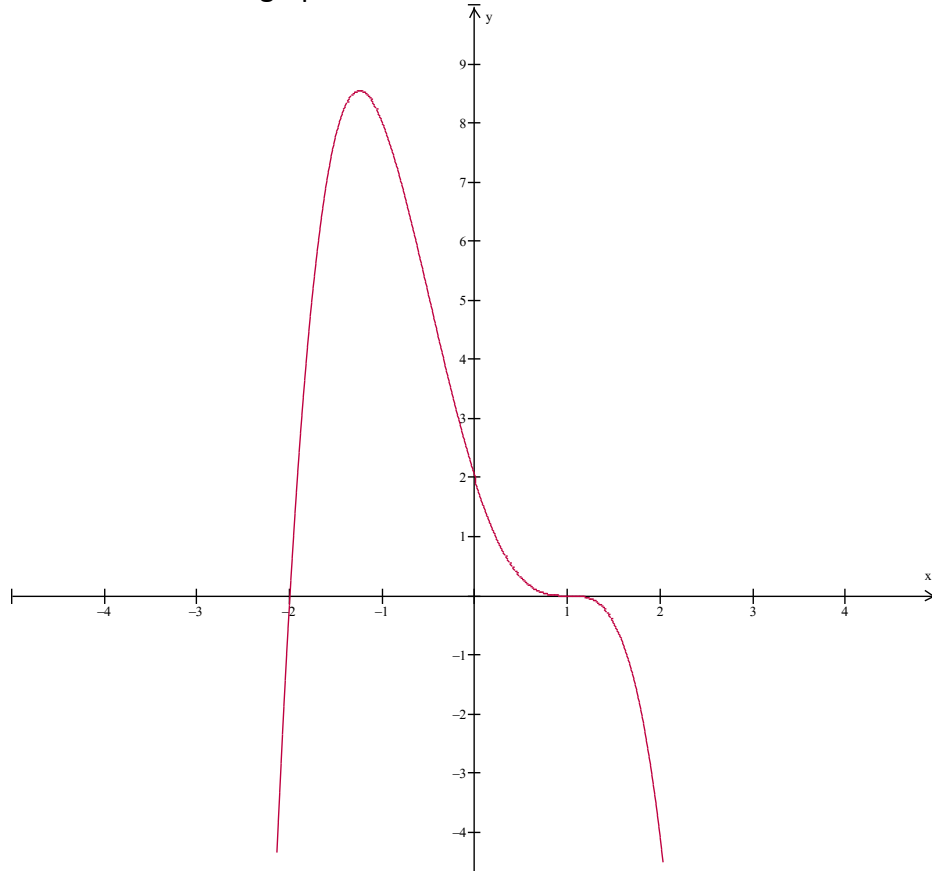
- a) The degree: 2
- b) Name of the polynomial function: QUADRATIC
- c) Leading coefficient: 7
- d) Constant term: 11

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3. Given the function $y = ax^n + 2x + b$, what are the conditions on a , n , and b for this function to have a range of all real numbers where the curve extends from up into quadrant 2 and down into quadrant 4 and has a positive y intercept? (3 marks)

$$\begin{aligned} a &< 0 \\ n &\text{ is odd} \\ b &> 0 \end{aligned}$$

4. Given the function graphed below:



- a) What degree is this function? (1 mark)

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- b) Is the leading coefficient positive or negative? (1 mark)

NEGATIVE

- c) How many different roots does this function have? (1 mark)

2

- d) The equation of the polynomial function. (2 marks)

$$y = -(x+2)(x-1)^3$$

5. Given the function $f(x) = x^3 + 3x^2 - x - 3$

(4 marks)

- a) Degree and end-behavior: 3 ^{1 mark} $\frac{1}{2}$ mark each
 LEFT: Down Q-403 RIGHT: UP Q 1
- b) The zeros and their multiplicity: $-3, -1, 1$ ALL MULTIPLICITY OF 1
- c) The y-intercept: -3

$$\begin{array}{c|cccc} & 1 & 3 & -1 & -3 \\ \hline x & 1 & 2 & -3 & 0 \end{array}$$

$$(x+1)(x^2+2x-3)$$

$$(x+1)(x+3)(x-1)$$

6. Determine the quotient:

(3 marks)

$$(2x^3 + x^2 - 2x + 1) \div (x + 2)$$

$$\begin{array}{r} 2x^2 - 3x + 4 \\ x+2 \overline{) 2x^3 + x^2 - 2x + 1} \\ \underline{2x^3 + 4x^2} \\ -3x^2 - 2x \\ \underline{-3x^2 - 6x} \\ 4x + 1 \\ \underline{4x + 8} \\ -7 \end{array}$$

$$\begin{array}{c|cccc} 2 & 2 & 1 & -2 & 1 \\ \hline & \downarrow & 4 & -6 & 8 \\ x & 2 & -3 & 4 & -7 \end{array}$$

$$= 2x^2 - 3x + 4 \quad \underline{-7}$$

$x+2$

7. Use the remainder theorem to determine the remainder when $-x^2 + 2x + 1$ is divided by $x + 2$. (1 mark)

$$\begin{aligned} R &= -(-2)^2 + 2(-2) + 1 \\ &= -4 - 4 + 1 \\ &= -7 \end{aligned}$$

8. When $x^3 + x^2 + kx - 15$ is divided by $x - 2$, the remainder is 3. Determine k . (2 marks)

$$\begin{aligned} 2^3 + 2^2 + 2k - 15 &= 3 \\ 8 + 4 + 2k &= 18 \\ 2k &= 6 \\ k &= 3 \end{aligned}$$

9. For the function $f(x) = x^3 - 13x^2 + 12$

a) List the possible integral factors. (1 mark)

$$\pm 1, \pm 2, \pm 3, \pm 4, \pm 6, \pm 12$$

b) Factor fully. (2 marks)

$$\begin{array}{r|rrrr} -1 & 1 & -13 & 0 & 12 \\ & & -1 & 12 & 12 \\ \hline & 1 & -12 & -12 & 0 \end{array} \quad (x-1)(x^2-12x-12)$$

10. Prove that $x^2 + 5x + 6$ is a factor of the polynomial:

$$P(x) = x^4 + 5x^3 + 2x^2 - 20x - 24$$

(3 marks)

$$x^2 + 5x + 6 = (x+3)(x+2)$$

$$P(-3) = 0$$

$$P(-2) = 0$$

\therefore SINCE BOTH ARE FACTOR, THEIR PRODUCT
WILL BE A FACTOR